

Write the sets in interval notation and sketch them on the number line.

1. (3pts) $\{x \mid x \leq 4\}$

$$\begin{array}{c} \text{-----}]_4 \\ (-\infty, 4] \end{array}$$

2. (3pts) $\{x \mid -2 < x < 0\}$

$$\begin{array}{c} \text{-----} (\\ -2 \qquad \qquad 0 \\ (-2, 0) \end{array}$$

Solve the equations.

3. (3pts) $2x - 4 = 7x - 2 \quad | +4$

$$\begin{array}{l} 2x = 7x + 2 \quad | -7x \\ -5x = 2 \quad | \div -5 \\ x = -\frac{2}{5} \end{array}$$

4. (4pts) $5 + 2(a - 3) = -3(a + 3)$

$$\begin{array}{l} 5 + 2a - 6 = -3a - 9 \\ 2a - 1 = -3a - 9 \quad | +3a \\ 5a - 1 = -9 \quad | +1 \\ 5a = -8 \quad | \div 5 \\ a = -\frac{8}{5} \end{array}$$

Simplify and write in standard form:

5. (4pts) $(x^2 - 5x + 2)(x - 3) = x^3 - 5x^2 + 2x - 3x^2 + 15x - 6$
 $= x^3 - 8x^2 + 17x - 6$

6. (4pts) $x^2(x + 4) - (x - 7)^2 = x^3 + 4x^2 - (x - 7)(x - 7)$

$$\begin{array}{l} = x^3 + 4x^2 - (x^2 - 7x - 7x + 49) \\ = x^3 + 4x^2 - x^2 + 14x - 49 \\ = x^3 + 3x^2 + 14x - 49 \end{array}$$

Simplify and write the answer so all exponents are positive:

7. (2pts) $y^6(3y)^4 = y^6 \cdot 3^4 y^4 = 81y^{10}$

8. (2pts) $\frac{(2x)^6}{x^4} = \frac{2^6 x^6}{x^4} = 64x^2$

9. (3pts) $(u^5 v^{-2})^4 u^{-7} v^7 = (u^5)^4 (v^{-2})^4 u^{-7} v^7 = u^{20} v^{-8} u^{-7} v^7 = u^{13} v^{-1} = \frac{u^{13}}{v}$

10. (5pts) $(4a^{-2}b^4)^3(a^5c^{-2})^{-4} = 4^3(a^{-2})^3(b^4)^3(a^5)^{-4}(c^{-2})^{-4}$
 $= 64a^{-6}b^{12}a^{-20}c^8 = 64a^{-26}b^{12}c^8$
 $= \frac{64b^{12}c^8}{a^{26}}$

11. (7pts) $\frac{(6x^5y^{-3})^3}{(2x^{-2}y^2)^4} = \frac{6^3(x^5)^3(y^{-3})^3}{2^4(x^{-2})^4(y^2)^4} = \frac{6 \cdot 6 \cdot 6 \cdot x^{15} y^{-9}}{2 \cdot 2 \cdot 2 \cdot 2 \cdot x^{-8} y^8} = \frac{27x^{23}y^{-17}}{2}$
 $= \frac{27x^{23}}{2y^{17}}$

Factor the following.

12. (4pts) $x^2 + 3x - 10 = (x+5)(x-2)$

prod = -10 5, -2
 sum = 3

13. (4pts) $x^2 - 10x + 24 = (x-6)(x-4)$

prod = 24 -6, -4
 sum = -10

Use the ac-method or another method to factor. Show how you got your answer.

14. (6pts) $2x^2 + 7x - 15 = 2x^2 + 10x - 3x - 15$ 15. (6pts) $4x^2 - 8x - 5 = 4x^2 - 10x + 2x - 5$

prod = -30 10, -3
 sum = 7
 $= 2x(x+5) - 3(x+5)$
 $= (2x-3)(x+5)$

prod = -20 -10, 2
 sum = -8
 $= 2x(2x-5) + 2x-5$
 $= (2x-5)(2x+1)$