

1. (21pts) For the following functions:

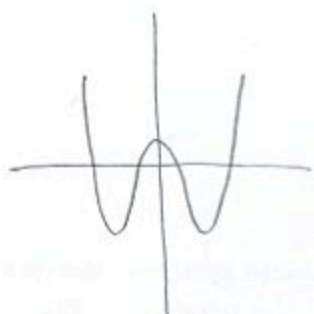
a) determine algebraically whether they are odd, even, or neither

b) use the calculator to draw their graphs here and verify your conclusions by stating symmetry.

$$f(x) = x^4 - 5x^2 + 2$$

$$\begin{aligned} f(-x) &= (-x)^4 - 5(-x)^2 + 2 \\ &= x^4 - 5x^2 + 2 = f(x) \end{aligned}$$

even



symm wrt y-axis

$$g(x) = \frac{x^5}{120} - \frac{x^3}{6} + x$$

$$\begin{aligned} g(-x) &= \frac{(-x)^5}{120} - \frac{(-x)^3}{6} + (-x) \\ &= -\frac{x^5}{120} - \frac{-x^3}{6} - x \\ &= -\frac{x^5}{120} + \frac{x^3}{6} - x = -g(x) \end{aligned}$$

odd



symm
wrt
origin

$$h(x) = x^3 - 7|x|$$

$$\begin{aligned} h(-x) &= (-x)^3 - 7|-x| \\ &= -x^3 - 7|x| \neq h(x) \\ &\neq -h(x) \end{aligned}$$

neither

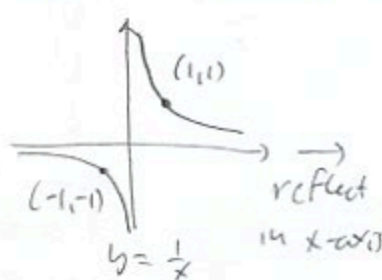


no symmetry

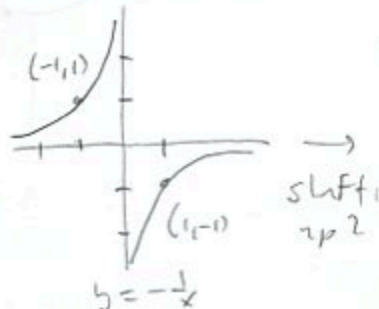
2. (16pts) Draw the graphs of $f(x) = 2 - \frac{1}{x}$ and $g(x) = -4\sqrt{-x}$ using transformations.

Explain how you transform graphs of basic functions in order to get the graphs of f and g .

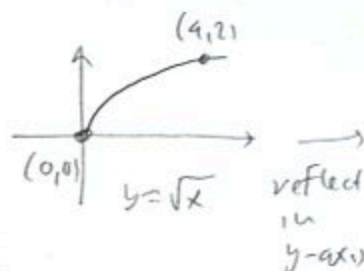
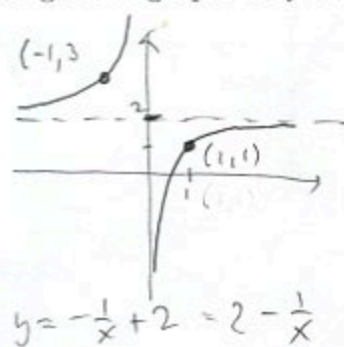
Indicate at least two points on each graph.



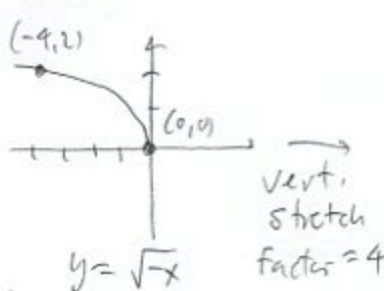
reflect
in x-axis



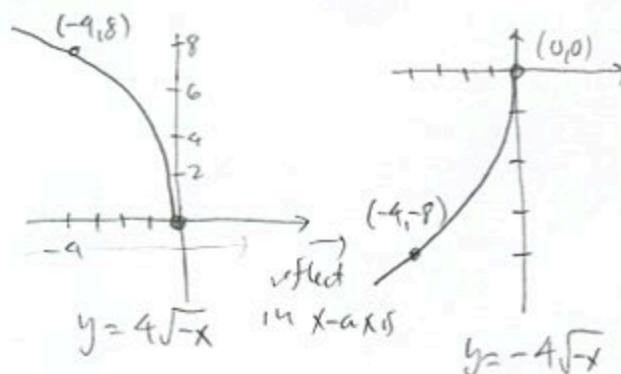
shift
up 2



reflected
in y-axis



vert.
stretch
factor = 4



reflect
in x-axis

$$y = -4\sqrt{-x}$$

3. (10pts) Write the equation for the function whose graph has the following characteristics:

a) shape of $y = \sqrt[3]{x}$, shifted right 4 units,

b) shape of $y = |x|$, reflected about the x -axis, then stretched horizontally by factor 2,

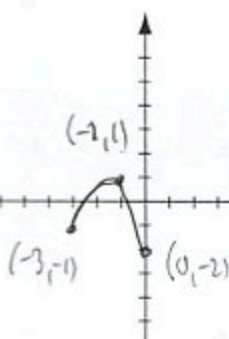
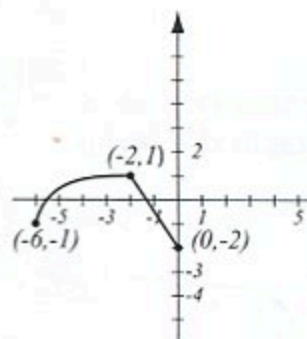
c) shape of $y = x^2$, reflected about the y -axis, then stretched vertically by factor 4, then shifted down 1 unit.

a) $\sqrt[3]{x} \rightsquigarrow \sqrt[3]{x-4}$

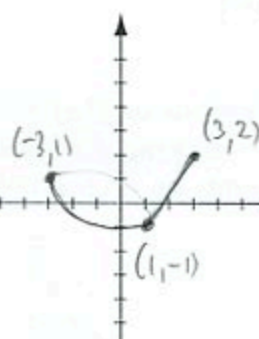
b) $|x| \rightsquigarrow -|x| \rightsquigarrow -|\frac{1}{2}x|$
(replace x by $\frac{1}{2}x$)

c) $x^2 \rightsquigarrow (-x)^2 \rightsquigarrow 4(-x)^2 \rightsquigarrow 4(-x)^2 - 1$
replace
 x by $-x$

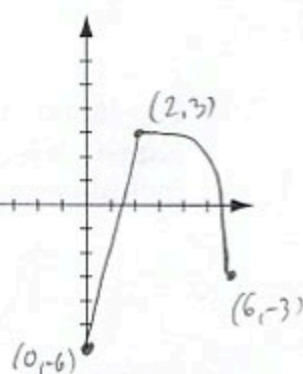
4. (13pts) The graph of $f(x)$ is drawn below. On separate coordinate systems, sketch the graphs of the functions $f(2x)$, $-f(x-3)$ and $3f(-x)$ and label all the relevant points.



horiz. stretch, factor $\frac{1}{2}$
 $x \mapsto \frac{1}{2}x$



shift right 3
reflect in x -axis
 $x \mapsto x+3$
 $y \mapsto -y$



reflect in x -axis
vert. stretch, factor 3
 $x \mapsto -x$
 $y \mapsto 3y$