## College Algebra — Exam 1 MAT 140C, Fall 2024 — D. Ivanšić

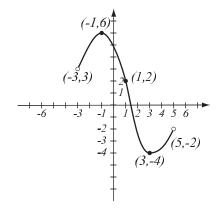
Name:

Show all your work!

1. (8pts) Use the graph of the function f at right to answer the following questions.

a) Find: 
$$f(-1) = f(5) =$$

- b) What is the domain of f?
- c) What is the range of f?
- d) What are the solutions of the equation f(x) = -3?



**2.** (12pts) Use your calculator to accurately sketch the graph of  $f(x) = -x^2 + 2x + 4$ .

- a) Draw the graph on paper and indicate units on the axes.
- b) Find all the x- and y-intercepts (accuracy: 6 decimal points).
- c) State the range of the function in interval notation.

**3.** (6pts) Find the equation of the line (in form y = mx + b) that passes through the points (-2, 1) and (1, -2). Draw the requested line.

**4.** (9pts) Find the equation of the line (in form y = mx + b) that is parallel to the line 3x + 2y = 8 and contains the point (1, -6). Draw both lines.

**5.** (7pts) In a coordinate system, draw the triangle with vertices A = (-1, 1), B = (3, 0), and C = (0, 5).

- a) Compute the slopes of the sides.
- b) Use slopes to determine if this is a right triangle.

**6.** (10pts) Let  $f(x) = \frac{1}{x^2 - 7x + 10}$ . Find the following (simplify where appropriate).

$$f(1) = f(2) =$$

$$f(a^3) = f(t-2) =$$

7. (5pts) Find the domain of the function below and write it using interval notation.

$$f(x) = \frac{4}{5 - 3x} - \frac{7}{3x + 4}$$

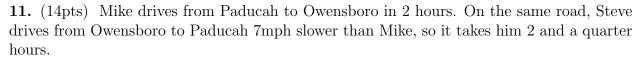
8. (7pts) Solve and write the solution in interval notation.

$$3 - x \ge 4$$
 or  $5 - 2x < 1$ 

- **9.** (10pts) The endpoints of a diameter of a circle are (1, -3) and (5, 1).
- a) Find the equation of the circle.
- b) Draw the circle in the coordinate plane.

- 10. (12pts) A water company offers two plans to pay for water:
- A) \$25 flat fee plus \$3 per cubic meter of water.
- B) \$35 flat fee that includes 2 cubic meters, and then \$2.50 per cubic meter for usage beyond 2 cubic meters.

Assuming a customer always uses at least 2 cubic meters of water per month, for which amount of water usage is plan A better? Solve as an inequality.



- a) How fast does Mike drive?
- b) What is the distance from Paducah to Owensboro along this road?

**Bonus** (10pts) Maria has a total of \$3500 invested in two accounts, one bearing 3% and the other 4% interest. The account bearing 4% gives \$12 more in interest in one year than the account bearing 3%. How much is invested in each account?