

4. How large must n be if the Composite Trapezoid rule is being used to estimate $\int_0^\pi \sin x \, dx$ with error $\leq 10^{-12}$? Will the estimate be too big or too small?

5. Consider $\int_1^2 \frac{dx}{x^3}$. What is the result of using the composite trapezoid rule with the partition points $1, \frac{3}{2}$, and 2 ?

6. We want to approximate $\int_1^2 f(x) \, dx$ given the table of values. Compute an estimate by the Composite Trapezoid rule. Can upper and lower sums be computed from the given data?

x	1	$\frac{5}{4}$	$\frac{3}{2}$	$\frac{7}{4}$	2
f(x)	10	8	7	6	5

7. Compute $\int_0^{0.35} \frac{2}{x^2-4} dx$ by the basic Simpson's Rule. Compare with the true solution.

8. Find an approximate value of $\int_1^2 x^{-1} dx$ using the basic Simpson's Rule with uniform spacing. Give a bound on the error.

9. Find an approximate value of $\int_{-2}^2 x^3 e^x dx$ using the Composite Simpson's Rule with uniform spacing with $n = 4$.

10. Find the constants c_0 , c_1 and x_1 so that the quadrature formula

$$\int_0^1 f(x) dx \approx c_0 f(0) + c_1 f(x_1)$$

gives exact results for all polynomials of degree at most 2.

11. Approximate

$$\int_0^2 e^{-x^2} dx$$

using the three point Gaussian Quadrature formula

$$\int_{-1}^1 f(x) dx \approx \frac{5}{9} f\left(-\sqrt{\frac{3}{5}}\right) + \frac{8}{9} f(0) + \frac{5}{9} f\left(\sqrt{\frac{3}{5}}\right).$$