

## Chapter 4 - Displaying and Summarizing Quantitative Data

August 25, 2010

### Graphs for Quantitative Data (LABEL GRAPHS)

**Histogram** (p.48) - Graph that uses bars to represent different frequencies or relative frequencies in specific intervals called classes or bins. The intervals are the same width and can be chosen for convenience. Look similar to Bar Charts, but there are no spaces between bars unless there is no data in that interval.

**Stem and Leaf Displays** (p. 50) - (Also called **Stem and Leaf Plots** or **Stem Plots**) Graph that is created by making a stem out of the left most digits and writing them in order in a vertical column. Then creating a leaf out of the right most digit and putting it in the row that corresponds to the appropriate stem. Leaves must be arranged in numerical order. This graph gives a quick picture of the distribution while including the numerical values.

If a row does not have any leaves to put in the stems must still be included to show where gaps might be.

If decimal values are used, the decimal values can be rounded.

**Example:** Length of ownership (in months) of cars before they are traded in.

72 15 70 40 42 74 64 68 50 53 62 64 45

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**Split Stem and Leaf Plot (p. 51)** - Plot that is created by splitting the stems into 2 or more rows. If 2 rows per stem than one will be used for digits 0-4 and the other for digits 5-9. This is useful for a larger sets or sets with large amounts of data in each row.

We will see **Back to Back Stem and Leaf Plots** in Chapter 5.

**Dotplots or Line Plot (p. 52)** – Graph constructed by placing a dot along the axis for each instance of a data value. Axis can be vertical or horizontal.

## Distributions for Graphs of Quantitative Variables

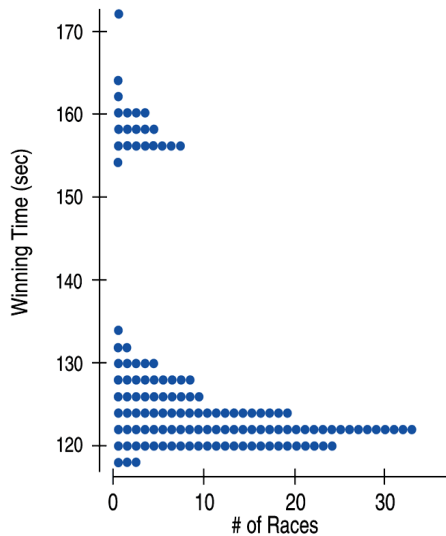
Whenever a distribution of a graph for a quantitative variable is described it should include its **shape**, **center**, and **spread**.

### Shape of a Distribution

- Is the graph **symmetric**, one side is close to the mirror image of the other or if folded along a vertical line through the middle the graph would match pretty closely.
- Is the graph **skewed**, which means one tail stretches out farther than the other. The graph is said to be skewed to the side of the longer tail
- Are there **peaks** or **modes** on the graph? This is where a large part of the data is occurring. **Unimodal** - one peak. **Bimodal** - two peaks. **Multimodal** - 3 or more peaks. **Uniform** if no peaks and fairly straight across graph.
- Are there any **outliers**, extreme values that are away from the rest of the data. Sometimes outliers will be ignored.
- Are there any **gaps** or spaces in the graph?

### Example:

Fig 4.4, p. 52 – Dotplot of Kentucky Derby winning times over the years.



### The Center of the Distribution: The Midrange and The Median

For a unimodal, symmetric distribution the **center** is the point on the graph where graph folds to give mirror image of each side.

What if the distribution is skewed or multimodal?

**Midrange (or Midpoint)** (p. 56) -  $\left( \frac{\text{Maximum Value} + \text{Minimum Value}}{2} \right)$ . Easy to

calculate, but it is very sensitive to extreme outlying values. It is not usually used to summarize a distribution.

**Median** (p.57) - Score in the middle when values are arranged in numerical order

If  $n$  is odd then median is in the  $\left( \frac{n+1}{2} \right)^{\text{st}}$  position

If  $n$  is even then median is the average of the numbers in the  $\left( \frac{n}{2} \right)^{\text{st}}$  position and

the  $\left( \frac{n}{2} + 1 \right)^{\text{st}}$  position.

**Example:**

10 25 30 35 40 60 60 65 100

10 25 30 35 40 60 60 65 80 100

The median is one of the many ways to find the center of the data. Another important way will be mentioned later.

### **The Spread of the Distribution: The Range and The Interquartile Range**

The **spread** measures how much the data varies from the center

**Range (p. 57)** - Maximum – Minimum. Sensitive to outlying values so does not always represent data properly.

Instead of looking at the ends of the data the range of the middle of the data could be measured.

**Interquartile Range (p. 58)** -  $IQR = Q_3 - Q_1$

Quartiles split the sorted data into Quarters.

The median is the middle quartile or  $Q_2$ .

The Third Quartile,  $Q_3$  or the Upper Quartile, is the median of the upper half of the numbers.

The First Quartile,  $Q_1$  or the Lower Quartile, is the median of the lower half of the numbers

The lower and upper quartiles are also known as the 25<sup>th</sup> and 75<sup>th</sup> percentiles, respectively.

(If n is odd the book includes the median in both halves when figuring up the quartiles. I will not, since that is the way the calculator leaves it out if n is odd.)

**Example:**

10 25 30 35 40 60 60 65 100

10 25 30 35 40 60 60 65 80 100

The **5-number summary** (p. 60) is the following

Minimum Score,  $Q_1$ , Median,  $Q_3$ , Maximum Score

### Summarizing Symmetric Distributions: Mean and Standard Deviation

If the distribution is symmetric then calculations for the center and spread can be used that include all data values.

**Mean**(p. 62) – The value found by summing up the numbers and dividing by n.

$$\bar{x} = \frac{\sum x}{n} = \frac{x_1 + x_2 + \cdots + x_n}{n}$$

Typically will see mean rounded to one more digit than data has.

**Example:**

10 25 30 35 40 60 60 65 100

Median is point where there are half of the scores above and half of the scores below. Median is not sensitive to outlying values.

Mean is point where histogram would “balance”. Mean is more sensitive to outlying values.

If distribution is symmetric then mean = median.

If distribution is skewed the mean is pulled closer to the tail than the median.

If distribution is symmetric and there are no outliers mean is preferred measure of center. If distribution is skewed or has outliers than median is preferred since the median is resistant to extreme large or small values.

### **Variance and Standard Deviation (p. 62)**

IQR only uses two quartiles (or 50%) of the data, so it ignores how individual values vary. The Standard Deviation takes into account how far each value is from the mean. These differences are called deviations.

$$\text{Variance: } s^2 = \frac{\Sigma(x - \bar{x})^2}{n - 1} \quad \text{Standard Deviation: } s = \sqrt{\frac{\Sigma(x - \bar{x})^2}{n - 1}}$$

Why ( )<sup>2</sup> each term?

Why Standard Deviation instead of Variance?

Like the mean the standard deviation is only appropriate for symmetric data.

Also as with the mean typically round standard deviation to one more digit than original data contains.

**Example:** Find the Standard Deviation of 1, 3, 4, 8, 9.

What to “Tell” about a Quantitative Variable (p. 66)

What can go wrong? (p. 69-71)