## College Algebra - Exam 1 MAT 140C, Fall 2021 - D. Ivanšić

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1. (8pts) Use the graph of the function $f$ at right to answer the following questions.
a) Find: $f(4)=\quad f(1)=$
b) What is the domain of $f$ ?
c) What is the range of $f$ ?
d) What are the solutions
of the equation $f(x)=-2$ ?

2. (10pts) Use your calculator to accurately sketch the graph of $y=x^{3}-8 x^{2}+5 x-3$.
a) Draw the graph on paper and indicate units on the axes.
b) Find all the $x$ - and $y$-intercepts (accuracy: 6 decimal points).
3. (5pts) Draw the line that passes through points $(-1,1)$ and $(-1,6)$. Then write the equation of the line.
4. (10pts) Find the equation of the line (in form $y=m x+b$ ) that is parallel to the line $2 x-4 y=5$ and passes through the point $(4,1)$. Draw both lines.
5. (8pts) Draw the quadrangle with vertices $A=(4,0), B=(2,4), C=(-4,0)$ and $D=(-2,-3)$. Use slopes to determine if any two of its sides are perpendicular.
6. (9pts) Let $f(x)=x^{2}-\sqrt{2 x-7}$. Find the following (simplify where appropriate). $f(1)=$

$$
f(8)=
$$

$f(4 u)=$

$$
f(x+3)=
$$

7. (9pts) Find the domains of the functions below and write them using interval notation.
$f(x)=\frac{1}{x^{2}-5 x-36}$
$g(x)=\sqrt{2 x+7}$
8. (5pts) Solve and write the solution in interval notation.
$4 \leq 7-2 x<11$
9. (10pts) The diameter of a circle has endpoints $(-2,-3)$ and $(4,1)$.
a) Find the equation of the circle.
b) Draw the circle in the coordinate plane.
10. (12pts) An electric company offers two plans to pay for electricity usage:
A) $\$ 60$ flat fee that includes 200 kWh , then 12 cents per kWh for usage beyond 200 kWh .
B) $\$ 10$ flat fee plus 16 cents per kWh .

Assuming a customer always uses at least 200 kWh of electricity, for which amounts of electricity is plan A better?
11. (14pts) Because she was afraid to be late, Fiona rushed to a concert and got there in 2 hours. On the way back, she drove 9 mph slower, so it took her a quarter of an hour longer. a) How fast did Fiona drive to and from the concert?
b) How far did she drive to the concert?

Bonus (10pts) The length of a rectangular field is 40 feet more than the width. A farmer used 470 feet of fencing to enclose the field and divide it into two parts, as in the picture. What are the dimensions of the field?


