Advanced Calculus 1 — Handout MAT 525/625 Fall 2023 — D. Ivanšić

Test Knowledge

Sections 1.1, 1.2, 1.3, 2.1–2.4

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Set bounded above/below, bounded, unbounded (2.3.1)

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Test Knowledge

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