College Algebra — Exam 1 MAT 140, Fall 2020 — D. Ivanšić

Show all your work!

1. (8pts) Use the graph of the function f at right to answer the following questions.

- a) Find: f(2) = f(-6) =
- b) What is the domain of f?
- c) What is the range of f?
- d) What are the solutions of the equation f(x) = 3?



2. (10pts) Use your calculator to accurately sketch the graph of $y = -x^3 + 8x + 12$.

a) Draw the graph on paper and indicate units on the axes.

b) Find all the x- and y-intercepts (accuracy: 6 decimal points).

3. (5pts) Write the equation of the line whose *x*-intercept is 3, and *y*-intercept is -5.

4. (10pts) Find the equation of the line (in form y = mx + b) that is perpendicular to the line x + 4y = -8 and passes through (2, -1). Draw both lines.

5. (8pts) Draw the triangle with vertices A = (0,0), B = (3,2) and C = (7,-4) in the coordinate plane. Use the Pythagorean theorem to determine if the triangle is a right triangle.

6. (9pts) Let $f(x) = x^2 + 4x - \frac{1}{\sqrt{x+1}}$. Find the following (simplify where appropriate). f(3) = f(-6) =

$$f(\sqrt{u}) = \qquad \qquad f(t-3) =$$

7. (9pts) Find the domains of the functions below and write them using interval notation.

$$f(x) = \frac{x-3}{2x-5} \qquad \qquad g(x) = \frac{\sqrt{5-3x}}{x+8}$$

8. (5pts) Solve and write the solution in interval notation.

 $-2 \leq 5-2x < 4$

9. (10pts) The diameter of a circle has endpoints (-3, 2) and (1, 0).

- a) Find the equation of the circle.
- b) Draw the circle in the coordinate plane.

10. (12pts) Ellen plans to invest \$12,000: part at 3.5% simple interest, and the rest at 4.5% simple interest. What is the most she can invest at 3.5% to guarantee receiving \$500 in interest in a year? Solve as an inequality.

11. (14pts) Amy and Mitch bicycle along the same road. It takes Mitch 1 hour to travel the road. Amy leaves 12 minutes after Mitch, but gets to the end of the road at the same time as Mitch because she travels 2 mph faster than him.

a) What are the speeds of the cyclists?

b) How long is the road?

Bonus (10pts) Let A = (1, 5) be a point in the plane. Find a point B on the x-axis so that the line through A and B is parallel to the line y = 3x - 1.