## College Algebra - Exam 1 MAT 140, Fall 2020 - D. Ivanšić

Name: $\qquad$ Show all your work!

1. (8pts) Use the graph of the function $f$ at right to answer the following questions.
a) Find: $f(2)=\quad f(-6)=$
b) What is the domain of $f$ ?
c) What is the range of $f$ ?
d) What are the solutions
of the equation $f(x)=3$ ?

2. (10pts) Use your calculator to accurately sketch the graph of $y=-x^{3}+8 x+12$.
a) Draw the graph on paper and indicate units on the axes.
b) Find all the $x$ - and $y$-intercepts (accuracy: 6 decimal points).
3. (5pts) Write the equation of the line whose $x$-intercept is 3 , and $y$-intercept is -5 .
4. (10pts) Find the equation of the line (in form $y=m x+b$ ) that is perpendicular to the line $x+4 y=-8$ and passes through $(2,-1)$. Draw both lines.
5. (8pts) Draw the triangle with vertices $A=(0,0), B=(3,2)$ and $C=(7,-4)$ in the coordinate plane. Use the Pythagorean theorem to determine if the triangle is a right triangle.
6. (9pts) Let $f(x)=x^{2}+4 x-\frac{1}{\sqrt{x+1}}$. Find the following (simplify where appropriate). $f(3)=$

$$
f(-6)=
$$

$$
f(t-3)=
$$

7. (9pts) Find the domains of the functions below and write them using interval notation.
$f(x)=\frac{x-3}{2 x-5}$

$$
g(x)=\frac{\sqrt{5-3 x}}{x+8}
$$

8. (5pts) Solve and write the solution in interval notation.
$-2 \leq 5-2 x<4$
9. (10pts) The diameter of a circle has endpoints $(-3,2)$ and $(1,0)$.
a) Find the equation of the circle.
b) Draw the circle in the coordinate plane.
10. (12pts) Ellen plans to invest $\$ 12,000$ : part at $3.5 \%$ simple interest, and the rest at $4.5 \%$ simple interest. What is the most she can invest at $3.5 \%$ to guarantee receiving $\$ 500$ in interest in a year? Solve as an inequality.
11. (14pts) Amy and Mitch bicycle along the same road. It takes Mitch 1 hour to travel the road. Amy leaves 12 minutes after Mitch, but gets to the end of the road at the same time as Mitch because she travels 2 mph faster than him.
a) What are the speeds of the cyclists?
b) How long is the road?

Bonus (10pts) Let $A=(1,5)$ be a point in the plane. Find a point $B$ on the $x$-axis so that the line through $A$ and $B$ is parallel to the line $y=3 x-1$.

