Mathematical Concepts - Final Exam
MAT 117, Fall 2012 - D. Ivanšić

Name:
e:

$$
\begin{aligned}
& I=P r t A=P(1+r t) \quad A=P\left(1+\frac{r}{n}\right)^{n t} \quad A=P \frac{\left(1+\frac{r}{n}\right)^{n t}-1}{\frac{r}{n}} \\
& P=P M T \frac{1-\left(1+\frac{r}{n}\right)^{-n t}}{\frac{r}{n}} \quad Y=\left(1+\frac{r}{n}\right)^{n}-1 \\
& \frac{a}{b}=\frac{P(E)}{1-P(E) \quad P(E)=\frac{a}{a+b} \text { where odds in favor of } E \text { are } a: b \quad P(B \mid A)=\frac{n(A \text { and } B)}{n(A)}} \begin{array}{l}
P(A \text { or } B)=P(A)+P(B)-P(A \text { and } B) \\
P(A \text { or } B)=P(A)+P(B)(\text { if } A \text { and } B \text { are mutually exclusive }) \\
P(A \text { and } B)=P(A) \cdot P(B \mid A) \quad P(A \text { and } B)=P(A) \cdot P(B) \text { if } A \text { and } B \text { are independent } \\
\text { midrange }=\frac{\text { lowest value }+ \text { highest value }}{2} \quad \text { range }=\text { highest value }- \text { lowest value } \\
\bar{x}=\frac{x_{1}+x_{2}+\cdots+x_{n}}{n}=\frac{\sum_{i} x_{i}}{n}=\frac{\sum_{i} f_{i} x_{i}}{n} \quad Z=\frac{X-\bar{x}}{s} \\
s=\sqrt{\frac{\left(x_{1}-\bar{x}\right)^{2}+\left(x_{2}-\bar{x}\right)^{2}+\cdots+\left(x_{n}-\bar{x}\right)^{2}}{n-1}}=\sqrt{\frac{\sum_{i}\left(x_{i}-\bar{x}\right)^{2}}{n-1}}=\sqrt{\frac{\sum_{i} f_{i}\left(x_{i}-\bar{x}\right)^{2}}{n-1}} \\
E=P_{1} \cdot A_{1}+P_{2} \cdot A_{2}+\cdots+P_{n} \cdot A_{n}
\end{array} \\
& \hline
\end{aligned}
$$

1. (24pts) A company is deciding where to take its employees for a "team-building" retreat. The choices are a cruise, Disney World and rafting. A poll of its middle managers results in the following preference rankings.
a) Which choice wins the vote in a plurality election?
b) Which choice wins the vote in a plurality election with elimination?
c) Which choice is the pairwise comparison winner?
d) Which choice is the winner using Borda's method?

Perform the check on the sum of Borda points.

| Votes: | 6 | 2 | 5 | 2 | 3 | 6 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: |
| 1st | C | C | D | D | R | R |
| 2nd | D | R | C | R | C | D |
| 3rd | R | D | R | C | D | C |

2. (12pts) Determine whether each of the following graphs has an Euler path or an Euler circuit. If it does, find it and state the order in which the vertices are visited, if not, explain why not.

3. (25pts) Over one month, a city public transportation employee counts how many of its buses break down in a day and comes up with the following data.
a) Draw a histogram for the data.
b) Find the mode number of buses broken down.
c) Find the median number of buses broken down.
d) Find the mean number of buses broken down.
e) Find the standard deviation.

| Buses <br> broken | Frequency <br> (days) |
| :---: | :---: |
| 0 | 3 |
| 1 | 11 |
| 2 | 9 |
| 3 | 5 |
| 4 | 2 |

4. (12pts) Psychologists administer a certain skill test and measure the time it takes subjects to complete it. They find that the times for completion are normally distributed with mean 17 seconds and standard deviation 1.5 seconds. Draw a picture showing which area you are computing as you answer:
a) What percentage of subjects completes the test in less than 16 seconds?
b) What percentage of subjects completes the test in between 18 and 19 seconds?
5. (12pts) Write the probabilities and odds against and in favor of the following events (you can show any work needed below):

|  | Event | probability | odds against | odds in favor |
| :--- | :---: | :---: | :---: | :---: |
| a) | Rolling sum 5 on a roll of two dice |  |  |  |
| b) | Drawing a king or a red ace from a deck of cards |  |  |  |
| c) | Getting more heads than tails on three coin tosses |  |  |  |

6. (6pts) Among 57 towns surveyed, 23 had a parking garage downtown and 31 had metered parking downtown, while 46 had a parking garage or metered parking downtown. If a random town is selected, what is the probability that it has both a parking garage and metered parking downtown?
7. (12pts) The following game of chance is offered to you. The cost to play is $\$ 1$ and you roll a die. If you roll a 3 , you win $\$ 3$, if you roll a 4 , you win $\$ 2$, and you win nothing in all other cases.
a) Compute the expected value of this game.
b) How much would you expect to win or lose if you played 60 games?
8. (10pts) In one year, there is a $7 \%$ chance of having a devastating hurricane in Atlantic City, NJ. Assuming that the appearance of hurricanes in different years are independent events, what is the probability that Atlantic City has a devastating hurricane
a) two years in a row?
b) at least once in three consecutive years?
9. ( 5 pts ) A nice pair of pants costs $\$ 90$. If purchased in Texas, where sales tax is $8.25 \%$, what is the total cost of the pants?
10. (10pts) You borrowed $\$ 2,000$ from a bank and repaid it with $\$ 2120$ after nine months. What was the interest rate on this loan?
11. (8pts) Rodrigo deposited $\$ 2800$ in an account with $3.25 \%$ interest, compounded quarterly. How much is in the account in three years?
12. (14pts) When she bought a home, Sandy took out a 25 -year $\$ 125,000$ mortgage at $3.25 \%$ compounded monthly.
a) What is her montly payment on the loan?
b) What are her total payments over the course of the loan? How much of this amount is for interest?

Bonus. (15pts) A mail carrier has to deliver mail to the neighborhood shown in the picture by parking at a corner and walking around the neighborhood. Houses are on both sides of the street, and the mail carrier always walks one row of houses on one side of the street at a time.
a) Draw a graph that models the neighborhood.
b) Can the mail carrier deliver the mail to every house in the neighborhood without walking by any row of houses twice and return to the starting point? If so, display the route.


