

- 3.** (20pts) Consider the region bounded by the curves $y = x^2$ and $y = \sqrt{x}$.
- Find the volume of the solid obtained by rotating this region about the y -axis.
 - Sketch the solid and a typical cross-section or cylindrical shell, depending on the method you are using.

- 4.** (12pts) The base of a solid is the disk bounded by the circle $x^2 + y^2 = 16$. The cross-sections of the solid perpendicular to the y -axis are rectangles whose height is $1/3$ of their width.
- Sketch the solid and a typical cross-section.
 - Set up the integral for the volume of the solid. Do not evaluate the integral.

5. (18pts) A tank is in the form of an upright circular cone with base radius 3m and height 15m (vertex is at top). Set up the integral for the work needed to fill this tank with water, assuming the water is raised from base level. Assume $g = 10$ and water density = 1000kg/m^3 . Do not evaluate the integral, but do draw copious pictures!

6. (16pts) Consider the function $f(x) = 1 - x^2$ over the interval $[-1, 1]$.

a) What is the average value of the function over the interval?

b) What is the geometric interpretation of average value? Sketch a picture.

c) Verify the conclusion of the Mean Value Theorem for integrals, that is, find values of c in the interval so that $f_{\text{ave}} = f(c)$.

Bonus (10pts) Consider the region from problem 2 again, but now rotate it around the vertical line $x = 3$.

- a) Set up the integral for the volume of the resulting solid. Do not evaluate the integral.
- b) Sketch the solid and a typical cross-section or cylindrical shell, depending on the method you are using.