## College Algebra - Exam 1 <br> MAT 140, Fall 2019 - D. Ivanšić

Name: $\qquad$ Show all your work!

1. (8pts) Use the graph of the function $f$ at right to answer the following questions.
a) Find: $f(-1)=\quad f(6)=$
b) What is the domain of $f$ ?
c) What is the range of $f$ ?
d) What are the solutions of the equation $f(x)=4$ ?

2. (10pts) Use your calculator to accurately sketch the graph of $y=x^{3}-4 x^{2}+x+15$.
a) Draw the graph on paper and indicate units on the axes.
b) Find all the $x$ - and $y$-intercepts (accuracy: 6 decimal points).
3. (5pts) A line contains the point $(1,-2)$. If you start at any point on the line, go right 3 units and then down 2 units, you wind up back on the line. Write the equation of the line.
4. (10pts) Find the equation of the line (in form $y=m x+b$ ) that is perpendicular to the line $3 x-y=2$ and passes through $(6,-3)$. Draw both lines.
5. (7pts) Draw the points $A=(3,4), B=(-1,5)$ and $C=(-2,0)$ in the coordinate plane. Use the distance formula to determine which of $A$ and $B$ is closer to $C$.
6. (9pts) Let $f(x)=x^{2}-\sqrt{3 x-11}+3$. Find the following (simplify where appropriate). $f(9)=$

$$
f(2)=
$$

$f\left(u^{2}\right)=$

$$
f(t+4)=
$$

7. (9pts) Find the domains of the functions below and write them using interval notation.
$f(x)=\sqrt{4 x-3}$

$$
f(x)=\frac{27 x+3}{x^{2}-2 x-15}
$$

8. (6pts) Solve and write the solution in interval notation.
$5-2 x<1$ or $9-4 x>6$
9. (10pts) A circle centered at $(-3,1)$ contains the point $(2,-1)$.
a) Find the equation of the circle.
b) Draw the circle in the coordinate plane.
10. (12pts) Cassandra is choosing a cell-phone provider on the basis of data plans, since service already includes unlimited talk and texting. Penny Phone charges $\$ 7.50$ per month plus $\$ 6$ per gigabyte of data. Data Boss charges $\$ 29$ per month, which includes 3 gigabytes of data, plus $\$ 4.50$ per gigabyte for data above 3 gigabytes. If Cassandra always uses more than 3 gigabytes a month, for which amounts of data is Penny Phone cheaper? Solve as an inequality.
11. (14pts) A steer and rodeo Steve's horse are running in the same direction. At start, the steer is 35 feet away and running at speed 9 feet per second. Steve is following on horse at 14 feet per second.
a) How long until Steve catches up with the steer?
b) How far do Steve and horse go until that moment?

Bonus (10pts) How many milliliters of a $40 \%$ solution of isopropyl alcohol must be mixed with 120 milliliters of an $80 \%$ solution of isopropyl alcohol in order to get a $65 \%$ solution of isopropyl alcohol?

