## College Algebra - Exam 1 <br> MAT 140, Fall 2014 - D. Ivanšić

Name: $\qquad$ Show all your work!

1. (8pts) Use the graph of the function $f$ at right to answer the following questions.
a) Find $f(3)$ and $f(0)$.
b) What is the domain of $f$ ?
c) What is the range of $f$ ?
d) What are the solutions of the equation $f(x)=4$ ?

2. (10pts) Use your calculator to accurately sketch the graph of $y=x^{3}-10 x-17$. Draw the graph here, and indicate units on the axes. Find all the $x$ - and $y$-intercepts (accuracy: 6 decimal points).
3. (4pts) Convert to scientific notation or a decimal number:

Use formulas to expand:
4. $(4 \mathrm{pts})(4 x+5)^{2}=$
5. (4pts) $\left(2 x-u^{2}\right)\left(2 x+u^{2}\right)=$
6. $(6 \mathrm{pts})$ Factor: $8 x^{3}-125=$

Simplify, showing intermediate steps. Assume variables can be any real numbers.
7. $(2 \mathrm{pts}) \sqrt[3]{108}=$
8. (5pts) $\sqrt{125 x^{7} y^{4}}=$
9. (8pts) Simplify.
$\frac{x-5}{3 x^{2}-x-10}-\frac{2 x}{x^{2}+3 x-10}=$
10. (8pts) Simplify. Express answers first in terms of positive exponents, then convert to radical notation.
$\frac{\left(x^{3} y^{-\frac{1}{2}}\right)^{\frac{3}{4}}}{\left(x^{\frac{2}{3}} y^{4}\right)^{\frac{1}{4}}}=$
11. ( 6 pts ) Rationalize the denominator.
$\frac{4-5 \sqrt{3}}{\sqrt{3}+2}$
12. (5pts) Solve the equation for $t$.
$c(a+b t)=d$
13. (8pts) Find the domain of the function $f(x)=\frac{1+\sqrt{x}}{x^{2}+2 x-8}$ and write it using interval notation.
14. (10pts) Let $g(x)=\left(x^{2}+2\right) \sqrt{3-x}$. Find the following (simplify where appropriate). $g(-1)$

$$
g(8)
$$

$g(\sqrt{a})$

$$
g(x-1)
$$

15. (4pts) Which of the following graphs are graphs of functions (yes/no)?

16. (8pts) A circle is centered at $(-3,4)$ and passes through the origin.
a) Find the equation of the circle.
b) Draw the circle in the coordinate plane.

Bonus (10pts) Find points on the $x$-axis whose distance to point $(3,2)$ is $\sqrt{29}$. Hint: what form do coordinates of points on the $x$-axis have?

