## College Algebra - Exam 1 <br> MAT 140, Fall 2012 - D. Ivanšić

Name: $\qquad$
Show all your work!

1. (8pts) Use the graph of the function $f$ at right to answer the following questions.
a) Find $f(-2)$ and $f(0)$.
b) What is the domain of $f$ ?
c) What is the range of $f$ ?
d) What are the solutions
of the equation $f(x)=1$ ?

2. (10pts) Use your calculator to accurately sketch the graph of $y=x^{4}-8 x^{2}-11$. Draw the graph here, and indicate units on the axes. Find all the $x$ - and $y$-intercepts (accuracy: 6 decimal points).
3. (4pts) Convert to scientific notation or a decimal number:
$27,110=$
$3.159 \times 10^{-5}=$

Use formulas to expand:
4. (4pts) $(3 x-2)^{2}=$
5. $(4 \mathrm{pts})\left(x^{2}-y\right)\left(x^{2}+y\right)=$
6. $(6 \mathrm{pts})(x+5)^{3}=$

Simplify, showing intermediate steps.
7. $(2 \mathrm{pts}) \sqrt{63}=$
8. $(5 \mathrm{pts}) \sqrt[3]{40 x^{4}}=$
9. $(7 \mathrm{pts}) \frac{\sqrt[4]{324 x^{5} y^{11}}}{\sqrt[4]{2 x y^{2}}}=$
10. (8pts) Simplify.
$\frac{2 x-1}{x^{2}-49}-\frac{4}{x^{2}+4 x-21}=$
11. (8pts) Simplify. Express answers first in terms of positive exponents, then convert to root notation.
$\frac{\left(64 x^{-2} y^{6}\right)^{\frac{2}{3}}}{\left(2 x^{-\frac{3}{5}} y^{5}\right)^{4}}=$
12. (6pts) Rationalize the denominator.
$\frac{4 \sqrt{2}-5}{3-\sqrt{2}}$
13. (4pts) Solve the equation for $y$.
$2 x+3 y=c$
14. (8pts) Solve the equation.
$3 x^{2}+5 x=6-x^{2}$
15. (4pts) Find the domain of the function $f(x)=\frac{|x-7|}{x+4}$.
16. (12pts) The circle whose diameter has endpoints $(5,1)$ and $(-1,-1)$ is given.
a) Find the equation of the circle.
b) Draw the circle in the coordinate plane.
c) Is this circle the graph of a function? Why or why not?

Bonus (10pts) Simplify.
$\frac{3+\frac{18 x^{2}-4 x}{x^{3}-8}}{1+\frac{10 x+44}{x^{2}+2 x-8}}=$

