

1. (4pts) Find the points symmetric to point $(-3, 4)$ with respect to:

x -axis

y -axis

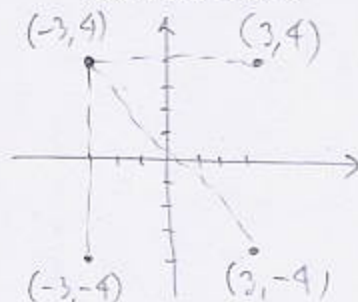
the origin.

Draw a picture.

$(-3, -4)$

$(3, 4)$

$(3, -4)$



2. (12pts) Check algebraically whether the graph of $y^2 - 3x = 5$ is symmetric with respect to the x -axis, y -axis, or the origin. Then use the calculator to draw the graph and verify your conclusions.

x -axis

y -axis

origin

$y^2 = 3x + 5$

$(-y)^2 - 3x = 5$

$y^2 - 3(-x) = 5$

$(+y)^2 - 3(-x) = 5$

$y = \pm \sqrt{3x + 5}$

$y^2 - 3x = 5$

$y^2 + 3x = 5$

$y^2 + 3x = 5$

same

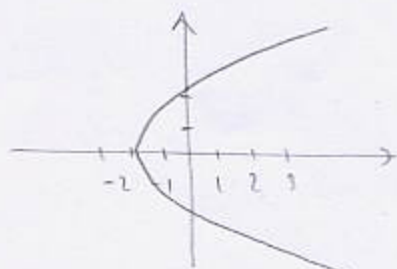
not same

not same

symm.

no symm.

no symm.



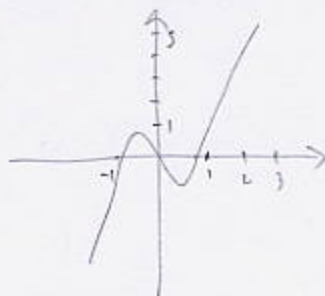
yes, symm. wrt x -axis

3. (14pts) For the following functions, determine algebraically whether they odd, even, or neither. Then use the calculator to draw their graphs and verify your conclusions.

$f(x) = 2x^3 - x$

$f(-x) = 2(-x)^3 - (-x) = 2(-x^3) + x$

$= -(2x^3 - x) = -f(x)$ odd



symm.

wrt

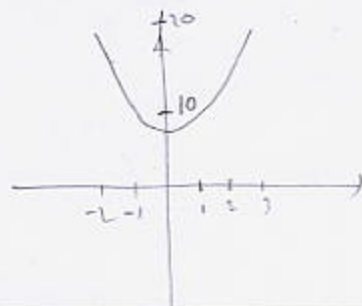
origin

so odd

$g(x) = x^2 + |x| + 7$

$g(-x) = (-x)^2 + |-x| + 7 = x^2 + |x| + 7 = g(x)$

even



symm.

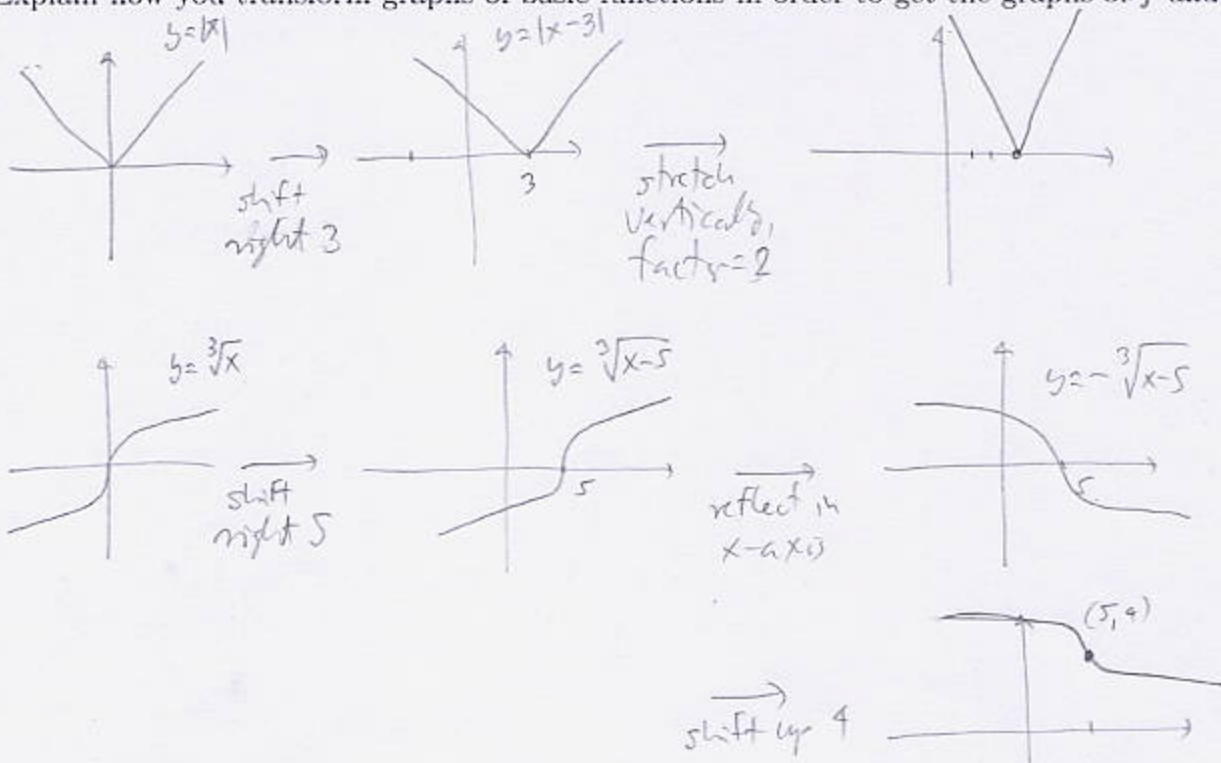
wrt

y -axis

so even

$$= -\sqrt[3]{x-5} + 4$$

4. (16pts) Using transformations, draw the graphs of $f(x) = 2|x-3|$ and $g(x) = 4 - \sqrt[3]{x-5}$. Explain how you transform graphs of basic functions in order to get the graphs of f and g .



5. (14pts) The graph of $f(x)$ is drawn below. On three separate graphs, sketch the graphs of the functions $f(x) - 1$, $f(3x)$ and $2f(-x)$ and label all the relevant points.

