Mathematical Concepts - Final Exam
MAT 117, Spring 2012 - D. Ivanšić
Name:
Show all your work!
$I=P r t A=P(1+r t) \quad A=P\left(1+\frac{r}{n}\right)^{n t} \quad A=P \frac{\left(1+\frac{r}{n}\right)^{n t}-1}{\frac{\pi}{n}}$
$P=P M T \frac{1-\left(1+\frac{r}{n}\right)^{-n t}}{\frac{1}{n}} \quad Y=\left(1+\frac{r}{n}\right)^{n}-1$
$\frac{a}{b}=\frac{(E)}{1-P(E)} \quad P(E)=\frac{a}{a+b}$ where odds in favor of $E$ are $a: b \quad P(B \mid A)=\frac{n(A \text { and } B)}{n(A)}$
$P(A$ or $B)=P(A)+P(B)-P(A$ and $B)$
$P(A$ or $B)=P(A)+P(B)($ if $A$ and $B$ are mutually exclusive $)$
$P(A$ and $B)=P(A) \cdot P(B \mid A) \quad P(A$ and $B)=P(A) \cdot P(B)$ if $A$ and $B$ are independent
$E=P_{1} \cdot A_{1}+P_{2} \cdot A_{2}+\cdots+P_{n} \cdot A_{n} \quad$ range $=$ highest value - lowest value
midrange $=\frac{\text { lowest value }+ \text { highest value }}{2} \quad$
$\bar{x}=\frac{x_{1}+x_{2}+\cdots+x_{n}}{n}=\frac{\sum_{i} x_{i}}{n}=\frac{\sum_{i} x_{i} f_{i}}{n} \quad Z=\frac{X-\bar{x}}{s}$
$s=\sqrt{\frac{\left(x_{1}-\bar{x}\right)^{2}+\left(x_{2}-\bar{x}\right)^{2}+\cdots+\left(x_{n}-\bar{x}\right)^{2}}{n-1}}=\sqrt{\frac{\sum_{i}\left(x_{i}-\bar{x}\right)^{2}}{n-1}}=\sqrt{\frac{\sum_{i} f_{i}\left(x_{i}-\bar{x}\right)^{2}}{n-1}}$

1. (24pts) Financial backers of the outdoor artist Christo are deciding in which world city his newest installation is to appear. They rank the three possible choices, Chicago, Kuala Lumpur and Naples in order of preference
a) Which choice wins the vote in a plurality election?
b) Which choice wins the vote in a plurality election with elimination?
c) Which choice is the pairwise comparison winner?
d) Which choice is the winner using Borda's method?

Perform the check on the sum of Borda points.

| Votes: | 4 | 2 | 5 | 3 | 7 | 2 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: |
| 1st | C | C | K | K | N | N |
| 2nd | K | N | C | N | C | K |
| 3rd | N | K | N | C | K | C |

2. (12pts) Determine whether each of the following graphs has an Euler path or an Euler circuit. If it does, find it, if not, explain why not.

3. (16pts) Systolic blood pressure readings are normally distributed with a mean of 121 and a standard deviation of 15 . Draw a picture showing which area you are computing as you answer:
a) What percentage of people have systolic blood pressure between 90 and 110 ?
b) What percentage of people have systolic blood pressure higher than 140 (which is considered high blood pressure)?
4. (24pts) A hospital keeps track of the number of days a patient stays in the hospital for an appendectomy. Below is the data.
a) Draw a histogram for the data.
b) Find the mode number of days spent.
c) Find the median number of days spent.
d) Find the mean number of days spent.
e) Find the standard deviation.

| Days <br> spent | Frequency <br> (patients) |
| :---: | :---: |
| 2 | 13 |
| 3 | 17 |
| 4 | 25 |
| 5 | 11 |
| 6 | 4 |

5. (12pts) Write the probabilities and odds against and in favor of the following events (you can show any work needed below):

|  | Event | probability | odds against | odds in favor |
| :---: | :---: | :---: | :---: | :---: |
| a) | Rolling a 3 on a single roll of a die |  |  |  |
| b) | Drawing a king or an ace from a deck of cards |  |  |  |
| d) | Getting sum 3 or 10 on a roll of two dice |  |  |  |

6. ( 6 pts ) The parking lot of a car dealership has 80 cars, of which 26 are used, 18 are silver, and 5 are used and silver. If a car is selected from the lot at random, what is the probability that it is used or silver?
7. (10pts) The probability that it will snow on Christmas in a certain Minnesota town is $45 \%$. Assume that whether it snows on Christmas in one year is independent of whether it snows on Christmas in any other year. What is the probability that it
a) snows on two Christmases in a row?
b) snows at least once on three Christmases in a row?
8. (12pts) An enterprising student devised this game of chance with his classmates in Dr. Smirf's class: a player pays $\$ 4$ to play and receives a prize if they guess the color Dr. Smirf's shirt the next day. The player wins $\$ 10$ if Dr. Smirf's shirt is red, $\$ 6$ if it is green, $\$ 3$ if it is black and nothing in all other cases. Suppose Dr. Smirf wears a red shirt on $10 \%$ of days, a green shirt on $20 \%$ of days, a black shirt on $30 \%$ of days, and a shirt of another color on other days.
a) Find the expected value of this game.
b) If a player played this game 30 times, how much would they expect to win or lose?
9. (6pts) Kristina borrowed $\$ 1,000$ from the bank at a $7 \%$ simple annual rate, and repaid the loan in 9 months. How much did she pay back?
10. (14pts) You would like to save up for a car.
a) How much should you deposit every quarter into an account with $5 \%$ interest, compounded quarterly, in order to have $\$ 15,000$ in four years?
b) How much of the final amount is from deposits and how much from interest?
11. (14pts) French president Sarkozy just lost his reelection bid. In an effort to console himself, he purchases a yacht for 1 million euros and takes out a 10-year loan for that amount at $6.6 \%$, compounded monthly.
a) What is his montly payment on the loan?
b) What are his total payments over the course of the loan? How much of this amount is for interest?

Bonus. (10pts) Below is a floor plan of a section of a museum, with doors joining rooms indicated.
a) Represent the floor plan as a graph (rooms are vertices, and don't forget to include one vertex for "outside").
b) Use the graph to determine if it is it possible to walk around the section, passing through every door exactly once. If it is, draw the route.
c) Is it possible to do the same as in b), and start and finish outside?


