| Mathematical Concepts - Exam 1 <br> MAT 117, Spring 2012 - D. Ivanšić |
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| Name: |
| $I=\operatorname{Prt} A=P(1+r t) A=P\left(1+\frac{r}{n}\right)^{n t} \quad A=P \frac{\left(1+\frac{r}{n}\right)^{n t}-1}{\frac{1}{n}} \quad P=P M T \frac{1-\left(1+\frac{r}{n}\right)^{-n t}}{\frac{1}{n}} \quad Y=\left(1+\frac{r}{n}\right)^{n}-1$ |

1. (10pts) a) 12 is what percent of 25 ?
b) 7 is $64 \%$ of what?
2. (10pts) You borrowed $\$ 400$ from a friend, and repaid him in 5 months with $\$ 450$. What simple annual interest rate did you pay on this loan?
3. (8pts) How much should you deposit in an account bearing $3.47 \%$, compounded semiannually, if you would like to have $\$ 4,000$ in three years?
4. (14pts) In 2010, single man Fidelio filed income taxes His total income was $\$ 85,300$, he deposited $\$ 5000$ into a retirement account, paid $\$ 7400$ in mortgage interest, $\$ 2100$ in property taxes, $\$ 3900$ in state income taxes and donated $\$ 750$ to charity. Use the table below to first determine Fidelio's taxable income (don't forget the exemption) and then find the tax on this income.

| Income bracket | Tax rate |
| :---: | :---: |
| up to $\$ 8,375$ | $10 \%$ |
| $\$ 8,376-\$ 34,000$ | $15 \%$ |
| $\$ 34,001-\$ 82,400$ | $25 \%$ |
| $\$ 82,401-\$ 171,850$ | $28 \%$ |
| $\$ 171,851-\$ 373,650$ | $33 \%$ |
| more than $\$ 373,650$ | $35 \%$ |
| exemption | $\$ 3650$ |

5. (14pts) You would like to save up for a nice new computer.
a) How much should you deposit every day into an account with $3.5 \%$ interest, compounded daily, in order to have $\$ 2,500$ in three years?
b) How much of the final amount is from deposits and how much from interest?
6. (32pts) True story: in an attempt at reducing Demi's anger at his indiscretions, Ashton bought her a very nice car for $\$ 103,000$. Made-up part: for this he took on a 7 -year loan at $5.25 \%$, compounded monthly.
a) What is his montly payment on the loan?
b) What are his total payments over the course of the loan? How much of this amount is for interest?
c) How much of his first payment goes toward interest, and how much towards the principal?
d) How much does he owe after 3 years?
7. (12pts) If you deposit $\$ 2000$ into an account bearing $11 \%$ interest, compounded quarterly, how long will it take until you have $\$ 6000$ in the account?

Bonus. (10pts) In an effort to save for a down payment on a home, Maria deposits $\$ 3000$ into an account, bearing $4.5 \%$, compounded monthly. Her financial situation does not allow her to make any additional deposits for a year. Then, after getting a promotion at work, she starts making monthly deposits of $\$ 200$ for the next two years into the same account. How much is in the account in three years from now?

