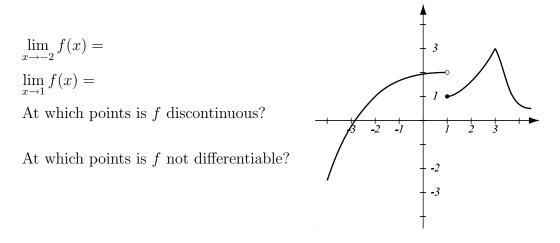
**1.** (6pts) Use the graph of the function to answer the following. Justify if a limit does not exist.



- **2.** (6pts) Find the limit  $\lim_{x\to 3} \frac{x^2 x 6}{x^2 + x 12}$  in two ways: a) algebraically
- b) Using L'Hospital's rule

**3.** (5pts) Use implicit differentiation to find y'.

$$x^2 + y^2 = x^2 y^2$$

4. (7pts) Let  $P(t) = 150e^{0.04t}$  be the population (in thousands) of a certain city at time t, measured in years.

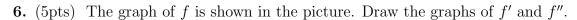
- a) What is the population t = 3?
- b) At what rate is the population increasing when t = 3? What are the units?
- c) Interpret the meaning of the number in b) by approximating the population at time t = 3.25.

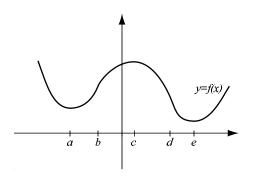
d) What is the exact population at time t = 3.25?

5. (9pts) Let  $f(x) = \frac{1}{x^2 + 4}$ .

a) Find the intervals of increase/decrease and where f has a local maximum and minimum. b) Find the intervals where f is concave up or down.

c) Use your calculator and the results of a) and b) to accurately sketch the graph of f.





7. (5pts) Let  $f(x) = \sqrt{x}$ . Find f'(x) using the definition of the derivative. Then compare to what you get using a differentiation rule.

8. (7pts) The line  $y = 8 - \frac{2}{3}x$  makes a triangle with the x- and y-axes. A rectangle may be inscribed in this triangle so that one vertex is on the line and two sides lie on the axes. Among all such rectangles, find the one that has the greatest area.

- 9. (6pts) Consider the integral  $\int_0^{\frac{2\pi}{3}} \cos x \, dx$ . a) Use a picture to determine whether this definite integral is positive or negative.
- b) Evaluate the integral and verify your conclusion from a).

10. (5pts) Use substitution (don't forget to change bounds) to evaluate:

$$\int_0^1 x^2 (1+2x^3)^5 \, dx =$$

**11.** (5pts) Simplify using part 1 of the Fundamental Theorem of Calculus. (Hint: if  $g(y) = \int_2^y t^2 \sin t \, dt$ , you are trying to find the derivative of  $g(y^2)$ . What is g'(y)?)

 $\frac{d}{dy}\int_{2}^{y^{2}}t^{2}\sin t\,dt =$ 

12. (4pts) Use the Intermediate Value Theorem to show that the equation  $e^x = x^2$  has a solution in [-2, 2].

**Bonus.** (7pts) A camera 5km away from the launch pad tracks a rocket as it lifts off. As the rocket moves upwards, the camera keeps it in its view. When the angle with the horizontal of the camera is  $\frac{\pi}{4}$  radians, the angle is increasing at rate 0.1 radians per second. What is the speed of the rocket at that moment?