

1. (4pts) Solve the equation:

$$x^2 - 6x + 7 = 0$$

2. (6pts) The line that passes through points  $(-1, 2)$  and  $(4, 0)$  is given.

a) Find the equation of this line.

b) Find the equation of the line perpendicular to the given one that passes through the point  $(1, 1)$ .

c) Sketch both lines on the same graph.

3. (4pts) Let  $f(x) = x^2 - 9$  and  $g(x) = x + 3$ . Compute the following (simplify where possible):

a)  $\frac{f}{g}(x) =$

b)  $(f \circ g)(x) =$

4. (7pts) The quadratic function  $f(x) = x^2 - 3x - 5$  is given. Do the following without using the calculator.

- a) Find the  $x$ -intercepts of its graph.
- b) Find the vertex of the graph.
- c) Sketch the graph of the function.

5. (6pts) Use the graph of the function  $f$ , below, to answer the following questions.

- a) What is  $f(2)$ ?
- b) Where is the function decreasing?
- c) Where does  $f$  have a local minimum? What is its value?
- d) How many solutions does the equation  $f(x) = 1.5$  have?
- e) What is the range of  $f$ ?

6. (4pts) Evaluate (do not use the calculator):

$$\log_4 64 =$$

$$\ln \frac{1}{e^2} =$$

$$\log_a(\sqrt[6]{a^7}) =$$

7. (4pts) Which of the following rates yields a larger amount in 1 year? (Hint: may use a principal of \$100 to compare.)

a) 4% compounded quarterly

b) 3.95% compounded monthly.

8. (4pts) The graph of  $f(x)$  is drawn below. Find the graphs of the other two functions and label all the relevant points.

$f(x)$

$f(x + 2)$

$\frac{1}{2}f(x)$

9. (10pts) Consider the rational function  $f(x) = \frac{x - 1}{(x + 3)(x + 1)}$ .

a) Find the domain of  $f$  and the vertical asymptotes of the graph.

b) Find the  $x$ -intercepts of the graph and the  $y$ -intercept.

c)  $f$  behaves like what function for large  $|x|$ ? What is the horizontal asymptote, if any?

d) Sketch the graph of the function on paper. Make sure scale is marked and all features you found in a)-c) are indicated.

10. (2pts) Use a formula to expand:  $(4x - 5)^2 =$

11. (3pts) Use a formula to factor:  $x^3 + 8 =$

12. (4pts) Simplify:  $\frac{2x - 1}{x^2 - 16} - \frac{x}{x^2 - x - 12} =$

13. (2pts) Rationalize the denominator

$$\frac{3}{5 + \sqrt{2}} =$$

14. (4pts) The population of Bunny Rapids was 10,552 in on 1/1/1998. Since then, the population  $P$  has grown according to the formula  $P = 10,552e^{0.035t}$ , where  $t$  is the number of years since 1/1/1998. In what year will population reach 13,000?

**15.** (6pts) How many milliliters of a 5% solution of sulphuric acid needs to be added to 200ml of a 20% solution in order to get a 15% solution? Don't forget to write down what your variable means.

**Bonus** (7pts) The price  $p$  and quantity  $x$  of electric grills sold at a store in a month obey the demand equation  $x = -20p + 500$ ,  $0 \leq p \leq 25$ .

a) Write the revenue  $R$  as a function of  $p$ . (Recall that  $R = xp$ .)

b) What price maximizes the revenue? How many grills are then sold?