

COLLEGE ALGEBRA - MAT 140

FALL 2008 - Review 5

I. True or False problems testing concepts.

II. Given that  $\log 5 = 0.699$  and  $\log 4 = 0.602$ , compute

- $\log 20$

- $\log 64$

- $\log \frac{1}{5}$

- $\log 0.2$

III. Write each expression as a sum and/or difference of logarithms. Express powers as factors.

- $\ln \left[ \frac{x^2 - x - 2}{(x + 4)^2} \right]^{\frac{1}{3}}, \quad x > 2$

- $\ln \frac{5x\sqrt{1+3x}}{(x-4)^3}, \quad x > 4$

IV. Write each expression as a single logarithm.

- $2 \log_2(x + 1) - \log_2(x + 3) - \log_2(x - 1)$

- $\log \left( \frac{x^2 + 2x - 3}{x^2 - 4} \right) - \log \left( \frac{x^2 + 7x + 6}{x + 2} \right)$

**V.** Solve the equations

- $2^{x+1} = 5^{1-2x}$

- $\ln(x+1) - \ln x = 3$

- $2^{2x} - 2^{x+2} - 12 = 0$

- $\log_{\frac{1}{3}}(x^2 + x) - \log_{\frac{1}{3}}(x^2 - x) = -1$

**VI.** Find the amount that results from each investment.

- \$500 invested at 8% compounded quarterly after a period of  $2\frac{1}{2}$  years.

- \$100 invested at 12% compounded continuously after a period of  $3\frac{3}{4}$  years

- \$200 invested at 9% compounded weekly after a period of  $2\frac{1}{4}$  years

**VII.** What rate of interest compounded annually is required to double an investment in 10 years?

**VIII.** Which is the better deal, 9% compounded quarterly or 9.24% compounded annually?

**IX.** How long will it take for an initial investment of \$10,000 to grow to \$25,000. Assume a rate of interest of 6% compounded continuously.